

## Example: Moore Machine<sub>JP</sub>

Define a Moore machine that facilitates counting the number of times the substring **aab** occurs in an input string over  $\Sigma = \{a, b\}$ . That is, the machine should output **1** if it has just read two **a** symbols followed by a **b**; otherwise it should output **0**.

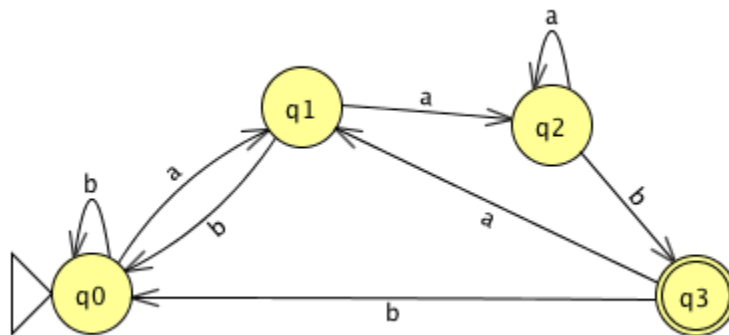
Recall that an Moore is defined as a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$  where

- $Q$  is a finite set of states, each of which specifies an output symbol
- $\Sigma$  is a finite alphabet of symbols for forming the input string
- $\Gamma$  is the finite set of symbols in the output alphabet
- $\delta$  is the transition function,  $\delta: Q \times \Sigma \rightarrow Q$
- $q_0$  is the start state ( $q_0 \in Q$ )

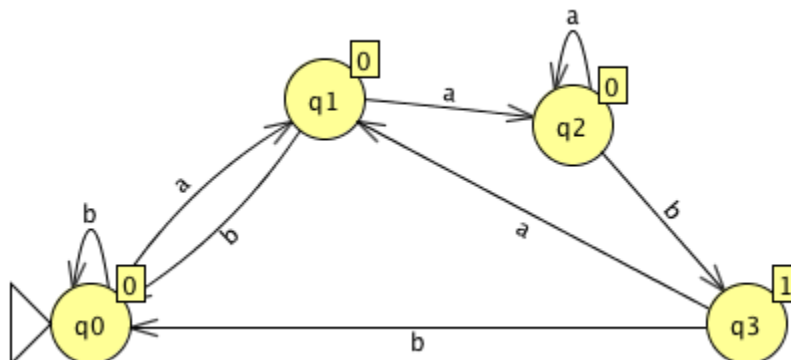
### Sample Solution

One approach is to consider a DFA that recognizes all strings that end with the specified substring. Then associate all states with output **0** except that machine's accept state which should be associated with the output **1**.

Here is a DFA that recognizes the set of all strings  $\{a, b\}^*$  that end with **aab** (see `DFA_aab.jff`).



Here is the Moore machine, based on that DFA, that prints a **0** except for state  $q_3$  which prints a **1**. (see `MOORE_aab.jff`).



Now step through input strings and observe the output. For example, the input string **aaababaabb** produces output **00001000010** indicating that there are exactly two occurrences of substring aab in the input.

